# **Etching of MgO crystals in acids: kinetics and mechanism of dissolution**

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Kinetics of etching of MgO crystals have been studied in  $H_2SO_4$ , HNO<sub>3</sub> and HCI. The effects of etching time, acid concentration and temperature on the growth of hillocks, on the selective etch rate and on the rate of overall dissolution are demonstrated. It is observed that etch rates are independent of time, but are determined by the temperature and concentration of the acid. The etch rate-concentration curves show maxima which are characteristic of an acid. The values of activation energy for the processes of **dissolution,** selective etching and hillock growth and the corresponding frequency factors are computed. It is established that the process of dissolution in concentrated  $H_2$  SO<sub>4</sub> is diffusion controlled, while in  $H_2$  SO<sub>4</sub> with concentrations below 18 N and in HNO<sub>3</sub> and HCl it is reaction rate controlled. The pre-exponential factor **is** found to be a function of acid concentration. The results are discussed from the standpoint of chemistry. A comment on the data published on MgO by previous workers is made.

## **1. Introduction**

Composition and temperature of an etching solution have profound influence on, *inter alia,*  the shape of etch features and on the dissolutionrate of crystals  $[1-11]$ . A study of the effect of etching parameters, especially those which can be controlled, e.g. temperature, composition and time, can serve as a source of valuable information about our scanty knowledge of the mechanism of dissolution of crystals. In metals and semiconductors the process of dissolution is fairly well understood [1, 2], but in alkali halides it remains unclear [3, 5]. The mechanism of dissolution of crystals of sparingly soluble salts, e.g.,  $CaF_2$ , MgO, BaSO<sub>4</sub>, etc., which are easily etched in dilute or concentrated acid solutions, is little studied  $[7, 9-11]$ .

Ghosh and Clarke [10] studied the influence of temperature on the dissolution rates of saturated solutions of  $NH_4Cl + H_2SO_4$  (1:1 ratio by volume) and  $88\%$  H<sub>3</sub>PO<sub>4</sub> on  $\{100\}$  faces of MgO crystals and calculated the parameters of etching. Sangwal and Sutaria [11] investigated the influence of concentration and temperature of different acid solutions on the formation of various surface features on {100} faces of MgO.  $O$  1978 Chapman and Hall Ltd. Printed in Great Britain.

However, both the hypothesis proposed for the mechanisms of the formation of various surface features [11], and the role of viscosity of the etching solution in the dissolution mechanism, require additional experimental investigations. The present article describes the effect of etching time, of etchant concentration and temperature on the overall dissolution rate and lateral etch rate at dislocations and hillocks formed on {100} faces of MgO crystals. The mechanism of dissolution is discussed in the light of the chemistry of the processes.

## **2. Experimental procedure**

The specimens were prepared in the form of parallelopipeds weighing between 0.3 and 0.8g with surface areas between 1.2 and  $2.8 \text{ cm}^2$ , from a large single crystal obtained from Norton Research Corporation, Canada. The samples were first polished in 33.08 N H<sub>3</sub>PO<sub>4</sub> at 100 to 110<sup>°</sup>C [11], then weighed to an accuracy of  $10^{-4}$  g. Thereafter their dimensions were measured employing a micrometer screw gauge with an accuracy of  $10^{-3}$  cm. They were then subjected to etching by placing them in 100ml beakers con-

TABLE I Weight loss, pit size and hillock size in 27N  $H<sub>2</sub>SO<sub>4</sub>$  at 21° C after 2h

Etching characteristics	Experiment I	Experiment II	
Weight loss $(X 10^{-3} \text{ g cm}^{-2})$	1.769	1.770	
Pit size $(\mu m)$	40	41	
Hillock size $(\mu m)$	$92 - 115$	$104 - 120$	

taining 30 to 35 ml of etching solutions at constant temperatures, with the long dimension either in a slanting position or vertical. Etching temperature was controlled within  $\pm$  0.5<sup>°</sup> C by using a constant temperature water bath whose temperature was regulated by a toluene temperature regulator operated by a magnetic relay system [12]. After specific durations, the samples were extracted



*Figure 1* Growth of hillocks in  $27 \text{ N H}_2$  SO<sub>4</sub> at  $21^{\circ}$ C for I h etching period. Some of the half-fflied hillocks are marked as A, while the completely filled ones as B (X 130).

*Figure 2* An example of single (marked S) and multiple (marked M) nucleation centres for growth of hillocks. Etching time 4 h, temperature  $21^{\circ}$  C ( $\times$  126).

from the beakers, rinsed under running water and dried with filter paper. They were then examined under an optical microscope and measurements of the size of etch pits (along  $(100)$ ) developed at the sites of fresh dislocations, and that of hillocks were taken at a magnification of  $\times$  100. After measurements and photography, the samples were re-weighed and the loss of weight by etching was calculated. The results are shown in Table I.

From 5 to 10 measurements of etch pit and hillock sizes, and from the loss in weight divided by the surface area of the sample, the lateral etch rate  $V_t$ , the rate of hillock growth  $V_h$  and the rate of overall dissolution  $V_d$  were calculated.

#### **3. Results**

# 3.1. Effect of etching time

The size of the hillocks was found to increase with the etching period. For shorter durations a good number of hillocks (Fig. 1) are underdeveloped and lack a morphology; but for longer durations they become completely filled and acquire a spherulite-like morphology (Fig. 2). On some of them even etch pits are developed, the size of which is always smaller than the size of the pits produced on the surface. A hillock can develop around one or more nucleation centres as seen in Fig. 2. Since multi-nucleation hillocks are larger than mono-nucleation hillocks, hillock size measurements were made only on mono-nucleation hillocks.

The curves of the time dependence of  $V_d$ ,  $V_t$ and  $V_h$  by etching  $\{100\}$  surfaces in 27 N H<sub>2</sub> SO<sub>4</sub> at  $21^{\circ}$ C are shown in Fig. 3. Apart from a short initial period, the rates are independent of time.



*Figure 3* Plots of (1) weight loss, (2) hillock size and (3) pit size versus etching time in 27 N H<sub>2</sub> SO<sub>4</sub> at 21 $^{\circ}$  C.



*Figure 4* (a) Plots of overall dissolution rate  $V_d$  and selective etch rate  $V_t$  versus  $H_2SO_4$  acid concentration c. Temperature of etching for curves 1 and 1', 21° C, 2 and 2', 45° C; 3 and 3', 60° C and 4 and 4', 77° C. Curves 1, 2, 3 and 4, and 1', 2', 3' and 4' are for dissolution and selective etch rates, respectively. (b) Graph of overall dissolution rate  $V_d$  and selective etch rate  $V_t$  versus HNO<sub>3</sub> and HCl concentration c. Points marked  $\circ$  and  $\bullet$  represent  $V_d$  and  $V_t$  respectively, for HCl acid at 24° C, while  $\bullet$  and  $\bullet$  stand for  $V_{\rm d}$  and  $V_{\rm t}$  respectively, for HNO<sub>3</sub> at 26° C.

#### 3.2. Effect of etchant concentration

The plots of  $V_d$  and  $V_t$  versus concentrations of  $H<sub>2</sub>SO<sub>4</sub>$ , HNO<sub>3</sub> and HCl are presented in Fig. 4. For a particular acid, the nature of the  $V_d-c$  and  $V_t$ –c curves is similar. The curves also show welldefined maxima, which are characteristic of a particular acid. In the case of  $HNO<sub>3</sub>$  and  $HCl$  (Fig. 4b), a well-defined peak is obtained at that acid concentration where circular etch pits are formed  $[11]$ . In H<sub>2</sub>SO<sub>4</sub> (Fig. 4a), a well-defined peak is observed at 18 N concentration when in addition to (1 0 0) etch pits, (1 0 0) pyramids at decorated dislocations are produced [11]. At low concentration a peak corresponding to circular etch pit formation in  $H_2$  SO<sub>4</sub> is also found.

# **3.3. Influence of** temperature *3.3.1. H2S04*

The plots of log  $V_d$ , log  $V_t$  and log  $V_h$  versus  $1/T$  (where  $T$  is temperature on the Kelvin scale)



*Figure 5* Plots of log  $V_d$  versus  $1/T$  for different H<sub>2</sub>SO<sub>4</sub> solutions:  $1-0.1$  N,  $2-0.5$  N,  $3-2$  N,  $4-5.5$  N,  $5 - 9$  N,  $6 - 18$  N,  $7 - 27$  N,  $8 - 36$  N.



*Figure 6* Plots of log  $V_t$  versus  $1/T$  for various  $H_2SO_4$ solutions:  $1 - 0.1 \text{ N}$ ,  $2 - 0.5 \text{ N}$  and  $2 \text{ N}$ ,  $3 - 5.5 \text{ N}$ ,  $4-9$  N,  $5-18$  N,  $6-27$  N and  $7-36$  N. Plot 8 represents  $\log V_{\rm h}$  versus  $1/T$ .



*Figure 7* Formation of hillocks by 36 N H<sub>2</sub>SO<sub>4</sub> at (a) 21<sup>°</sup> C and (b) 77<sup>°</sup> C. Time of etching (a) 1 h and (b) 11 min  $(X 120)$ .

in the interval 20 to  $80^{\circ}$  C are shown in Figs. 5 and 6. Except at 27 N and  $36$  N  $H_2$  SO<sub>4</sub>, the dependence of  $\log V_d$  on  $1/T$  can be approximated to parallel straight lines in the whole temperature interval for all the acid concentrations. This suggests that the value of the activation energy for overall dissolution,  $E_d$ , is constant but that of the pre-exponential factor, *Aa,* is dependent on the concentration of the etchant. In the temperature interval between 20 and  $60^\circ$  C,  $E_d$  for 27 N H<sub>2</sub>SO<sub>4</sub> is less than that for lower  $H_2SO_4$  concentrations. In the same interval the value of  $E_d$  for 36 N H<sub>2</sub> SO<sub>4</sub> is higher than that of  $27 \text{ N H}_2 \text{ SO}_4$ . Above 60°C, the behaviour of 27 N and 36 N  $H_2$  SO<sub>4</sub> solutions is quite different; for the former  $E_d$  increases, whereas in the latter it becomes negative.

The trend of the  $\log V_t$  versus  $1/T$  curves for  $H_2$  SO<sub>4</sub> concentrations lower than 18 N is similar to that for the overall dissolution process. For 18 N, 27 N and 36 N  $H_2$  SO<sub>4</sub>, the curves show a difference in the temperature interval 20 to  $60^{\circ}$  C.

The curve of log  $V<sub>h</sub>$  versus  $1/T$  for  $27 N H<sub>2</sub> SO<sub>4</sub>$ solutions (plotted in the upper part of Fig. 6) shows that the process is activation controlled. For 36 N solution, this dependence is irregular as is shown by the points. A comparison of the photographs of the surface features formed by 36N  $H<sub>2</sub>SO<sub>4</sub>$  solutions at different temperatures, illustrated in Fig. 7, shows that at higher temperature the density of hillocks has considerably increased.

The values of  $E_{d}$ ,  $E_{t}$ ,  $E_{h}$ , and the corresponding A's are given in Table II.

N	$E_{\bf d}$ (eV)	$E_{\pm}$ (eV)	$E_{\bf h}$ (eV)	$A_{\mathbf{d}}$ $(g \, \text{cm}^{-2} \, \text{h}^{-1})$	$A_{\rm t}$ $(\mu m h^{-1})$	$A_{\bf h}$ $(\mu m h^{-1})$
0.1	0.59	0.65		$2.61 \times 10^{6}$	$3.69 \times 10^{11}$	mar.
0.5	0.59	0.65		$3.98 \times 10^{6}$	$5.01 \times 10^{11}$	
2.0	0.59	0.65		$4.82 \times 10^{6}$	$5.01 \times 10^{11}$	
5.5	0.59	0.65		$6.43 \times 10^{6}$	$6.59 \times 10^{11}$	
9.0	0.59	0.65		$9.44 \times 10^{6}$	$1.04 \times 10^{12}$	
18.0	0.59	0.35		$1.57 \times 10^{7}$	$1.26 \times 10^{12}$	
		$0.65$ <sup>*</sup>			$2.19 \times 10^{7}$	
27.0	0.20	0.35	0.65	$1.53 \times 10^{6}$	$8.25 \times 10^{6}$	$7.22 \times 10^{12}$
	(0.59)	$(-0.23)$		$(2.15 \times 10^6)$	(16.5)	
36.0	0.31	0.06		$1.47 \times 10^{2}$	24.2	
	$(-0.19)$			$(4.64 \times 10^{-6})$		
0.5	0.59	0.68		$3.83 \times 10^{6}$	$1.75 \times 10^{12}$	
6.0	0.59	0.68		$3.83 \times 10^{6}$	$6.52 \times 10^{10}$	
0.5	0.59	0.68		$3.83 \times 10^{6}$	$1.75 \times 10^{12}$	
6.0	0.59	0.56		$3.83 \times 10^{6}$	$3.40 \times 10^{10}$	
	Normality					

TABLE II Activation energy and pre-exponential factor for various solutions

\*The values of  $E_d$ ,  $E_t$ ,  $A_d$  and  $A_t$  given in brackets correspond to the higher temperature region. 1980



*Figure 8* Log  $V_d$  and log  $V_t$  versus 1/T plots for  $\bullet$  – 0.5 N HNO<sub>3</sub>,  $\blacktriangle$  - 6 N HNO<sub>3</sub>,  $\circ$  - 0.5 N HCl and  $\triangle$  - 6 N HCl. Curve 1 is for overall dissolution while curves 2, 3 and 4 are for selective etching.

# 3.3.2. HNO<sub>3</sub> and HCI

The dependence of log  $V_d$  and log  $V_t$  versus  $1/T$ for  $0.5$  N and  $6$  N solutions of  $HNO<sub>3</sub>$  and HCl in the same temperature interval is shown in Fig. 8. If the scatter in the points is ignored, the value of  $E_d$ is 0.59 eV. The values of activation energy and preexponential factor for different solutions of  $HNO<sub>3</sub>$ and HC1 are also included in Table II.

#### **4. Discussion**

Dissolution of a surface may be considered to involve five consecutive steps [13] :

(1) Diffusion of the reacting molecules to the surface.

(2) Adsorption of the reacting molecules on the surface.

(3) Reaction on the surface.

(4) Desorption of the reaction products.

(5) Diffusion of the desorbed products into the solution.

Steps 1 and 5 of the transport of the reacting and reacted species are determined by diffusion kinetics, whereas 2, 3 and 4, which are usually regarded as a single step, are limited by the reaction rate between the acid and the solid. Since the dissolution rate is determined by the slowest step, the process of dissolution may be diffusion controlled or reaction rate controlled, depending on the conditions of the experiment.

Let us first analyse the temperature dependence of dissolution rates. Examination of log  $V_d$  and log  $V_t$  versus  $1/T$  curves shows that the processes of dissolution exhibit similar dependence although the etching parameters are different in the two cases (Table II). In particular, the values of *Ea*  vary markedly at  $27 \text{ N}$  and  $36 \text{ N}$  H<sub>2</sub> SO<sub>4</sub> concentrations, and there are instances when, at a particular concentration (e.g. at 27 N above 60 $\degree$ C),  $E_d$  is positive and  $E_t$  is negative. The lower values of  $E_d$ and  $E_t$  at 27 N and 36 N  $H_2$  SO<sub>4</sub> concentrations in comparison with those  $\leq 18 \text{ N}$  suggest that at higher concentrations the process may be diffusion limited.

With an increase in the concentration of an acid, its degree of dissociation is appreciably reduced, but it remains constant with temperature [14]. Consequently, at a particular acid concentration, it can easily be found out whether or not the dissolution process is diffusion controlled by plotting log  $\sigma$  (where  $\sigma$  is viscosity of the solution) versus *1/T* in the temperature interval of interest. For liquids which have a low viscosity at room temperature, the value of activation energy for the viscosity decrease,  $E_a$ , is usually  $0.14 \text{ eV}$  (see Table III). On the other hand for denser solutions, the curves of log  $\sigma$  versus  $1/T$  (Fig. 9) always have two slopes, each corresponding to relatively high values of activation energy. It should be noted that the value of  $E_{\sigma}$  is not connected with the degree of dissociation of the solution. In general, the acti-

TABLE III Activation energy for the rate of viscosity decrease with temperature for various solutions

Liquid	Viscosity at 20 $^{\circ}$ C σ		Activation energy $E$ (eV)	Degree of dissociation at $18^{\circ}$ C
CH, OH	$0.597$ cP		0.11 <sup>a</sup>	
C,H, OH	1.200cP		0.15 <sup>a</sup>	
<b>HCOOH</b>	$1.804$ cP		0.15 <sup>a</sup>	
CH, COOH	$1.26$ cP		$0.14^{a}$	0.004
36 N H <sub>2</sub> SO <sub>4</sub>	25.4	$_{\rm cP}$	$0.19, 0.27$ <sup>ac</sup>	0.57
H, O	$\cdot$ 1.0	cS	$0.14^{b}$	
$2.21 - 13.23$ N				
$H_3PO_4$	$1.0 - 2.2$ cS		$0.14^{b}$	
22.05 N H <sub>2</sub> PO <sub>4</sub>	4.3	cS	$0.14, 0.21^{\rm b}$	
33.08 N H <sub>3</sub> PO <sub>4</sub>	15.0	cS	$0.19, 0.26^{\rm b}$	
37.50 N H <sub>3</sub> PO <sub>4</sub>	28.0	cS	$0.21, 0.29^{\rm b}$	
44.10 N H <sub>3</sub> PO <sub>4</sub>	140.0	cS	$0.22, 0.39^{\rm b}$	0.17

 $a$  calculated from the data of  $[15]$ .

 $<sup>b</sup>$  calculated from the data of [16].</sup>

e the two values correspond to temperature interval above and below  $45^\circ$  C.



*Figure 9* Dependence of viscosity  $\sigma$  of H<sub>3</sub>PO<sub>4</sub> and H<sub>2</sub>SO<sub>4</sub> on temperature  $T: 1 - H_2 O$ ,  $2 - 2.21 N H_3 PO_4$ ,  $3 - 8.82$  $N H_3PO_4$ , 4 - 13.23 N  $H_3PO_4$ , 5 - 22.05 N  $H_3PO_4$ , 6 - $33.08 \text{ N H}_3\text{PO}_4$ ,  $7 - 37.50 \text{ N H}_3\text{PO}_4$ ,  $8 - 44.10 \text{ N H}_3\text{PO}_4$ and  $9 - 36$  N H, SO<sub>4</sub>.

vation energy increases with the concentration of the acid. The  $E_d$  values of 0.31 eV and 0.20 eV for  $36\text{ N}$  and  $27\text{ N}$  H<sub>2</sub>SO<sub>4</sub> at temperatures below  $60^{\circ}$ C may thus be attributed to the diffusion limited dissolution kinetics. Similar behaviour has also been reported for Ge and Si crystals [17].

The high values of *Ea* in dilute solutions of  $H<sub>2</sub> SO<sub>4</sub>$  and different solutions of  $HNO<sub>3</sub>$  and HCl is obviously connected with chemically controlled dissolution kinetics.

In the lower temperature interval for 18N, 27 N and 36 N  $H_2$  SO<sub>4</sub>,  $E_t$  has values of 0.35, 0.35, 0.06eV, respectively. This indicates that the process of dislocation etching could well be diffusion controlled or, in particular for 18N and 27N  $H<sub>2</sub>SO<sub>4</sub>$  it could be controlled by both diffusion as well as reaction rate processes. At lower  $H_2$  SO<sub>4</sub> concentrations and at different  $HNO<sub>3</sub>$  and HCl concentrations, the kinetics of selective etching are limited by reaction rate. However, in some cases, as for example during selective etching in  $18 \text{ N H}_2$  SO<sub>4</sub> and during overall dissolution in 27 N  $H<sub>2</sub> SO<sub>4</sub>$ , the kinetics appear to have switched over from diffusion controlled to chemically controlled ones. The negative values of  $E_d$  in 36 N H<sub>2</sub>SO<sub>4</sub> and of  $E_t$  in 27 N  $H_2$  SO<sub>4</sub> above 60° C seem to be connected with the instability of the reaction products. Indeed, the photograph of Fig. 7b points to this possibility.

For concentrations lower than  $18 \text{ N H}_2\text{SO}_4$ ,  $E_d \leq E_t$ . This difference, though small, may be attributed to the localization of energy around

dislocations. Whenever the condition  $E_d \ge E_t$ prevails, and if etch pits are formed at some stage with the increase of temperature, the pits disappear (compare the curve for  $36$  N  $H<sub>2</sub>SO<sub>4</sub>$  of Figs. 5 and 6).

The curves of log  $V_d$  and log  $V_t$  versus  $1/T$  for  $0.5$  N and  $6$  N HNO<sub>3</sub> and HCl acids show a behaviour similar to that of  $0.5$  N and  $5.5$  N  $H<sub>2</sub>SO<sub>4</sub>$ acid. The value of  $E_d$  in the case of  $HNO_3$  and  $HCl$ is equal to  $E_d$  in 5.5 N H<sub>2</sub>SO<sub>4</sub>. The value of  $E_t$  for  $0.5$  N HCl,  $0.5$  N HNO<sub>3</sub> and  $6$  N HNO<sub>3</sub> is equal to  $0.68$  eV, but that for 6 N HCl is  $0.56$  eV. These values differ from the values of  $E_t$  corresponding to  $0.5$  N and  $5.5$  N  $H_2$  SO<sub>4</sub> solutions. In  $0.5$  N HCl, 0.5 N HNO<sub>3</sub> and 6 N HNO<sub>3</sub> where  $E_d \le E_t$ , pits retain their contrast but where  $E_d > E_t$  they become invisible. When various solutions have the same values of  $E_d$  and  $E_t$ , the dissolution rates are determined by the values of the frequency factor  $\overline{A}$  (Table II, Figs. 5, 6 and 8).

We now attempt to explain the mechanism of dissolution from the standpoint of chemical kinetics. The system under consideration is one in which the processes of diffusion, adsorptiondesorption and chemical reaction all take part. Let us write down the chemical reactions [11] :

$$
MgO + 2H_2SO_4 \to Mg(HSO_4)_2 + H^+ + OH^-
$$

$$
(1)
$$

$$
Mg(HSO_4)_2 + OH^- \rightarrow MgOH^+ + 2HSO_4
$$

(2)

$$
MgOH^{+} \longrightarrow MgO + H^{+} (3)
$$

The first equation represents the formation of the reaction products, while the latter two represent the formation of hillocks in concentrated  $H_2SO_4$ and HCOOH and weak  $H_3PO_4$ . If the reactions proceed as represented above, it may be possible to observe the formation of some insoluble reaction products under certain conditions. This may happen especially at high concentrations of the solution when the sulphate and hydrosulphate are soluble only in alkalis, glycerol and ether [15]. Actually in concentrated  $H_2SO_4$ , after sufficiently long durations of etching, it is observed that the appearance of the liquid surrounding the crystal becomes milky. If the behaviour of  $Mg(HSO_4)_2$  and  $Mg(OH)_2$  (formed by the union of OH<sup>-</sup> ions present in the solution with  $MgOH<sup>+</sup>$  of Reaction 2) is taken into consideration from the viewpoint of their solubility in water, the likely compound is  $Mg(OH)_2$ . Indeed, this product remains to be identified chemically. However, from the observations that the hillocks grow with time, and that the size of etch pits on the surfaces of hillocks is always smaller than that on the surface, it is certain that back reaction leading to the formation of MgO from  $Mg(HSO<sub>4</sub>)<sub>2</sub>$  takes place.

In the state of equilibrium, Equation 1 may be written as

$$
MgO + 2H_2SO_4 \xrightarrow[K_6]{K_f} Mg(HSO_4)_2 + H_2O \quad (4)
$$

where  $K_f$  and  $K_b$  are the rate constants in the forward and the backward directions, respectively. Then the dissolution rate  $V$  may be expressed as

$$
V = K_{\mathbf{f}} [\text{HSO}_4]^2 - K_{\mathbf{b}} [\text{Mg}(\text{HSO}_4)_2]
$$
  
or 
$$
V = [K_{\mathbf{f}} - K_{\mathbf{b}} K_1] [\text{H}_2 \text{SO}_4]^2
$$
 (5)

taking  $[Mg(HSO_4)_2] = K_1[H_2SO_4]$ .

For dilute solutions,  $K_{\rm b} = 0$ , and hence

$$
V = K_{\mathbf{f}} \left[ \mathrm{H}_2 \, \mathrm{SO}_4 \, \right]^2, \tag{6}
$$

which implies that if  $K_f$  is independent of concentration,  $V \propto [H_2 SO_4]^2$ , and that at a particular concentration when  $K_f$  or  $(K_f - K_b K_l)$  is constant, the weight loss, growth of pit or hillock size should increase linearly. The curves shown in Fig. 3 support the above conclusion. A rapid initial increase in the curves is associated with the establishment of an equilibrium at the crystal surface [18].

An examination of  $V$  versus  $c$  curves for various acids shows that in  $H_2SO_4$  the concentration dependence of etch rates is initially quite weak, but later is is quite marked. In  $HNO<sub>3</sub>$  and  $HCl$ somewhat different behaviour is observed. The value of  $n$ , defined as the order of the reaction by an expression  $V=Kc^n$ , where c is the concentration of the acid, is about 1 in the range of 9 to 18 N  $H_2SO_4$ , 0.5 to 1.5 N HCl and 0.5 to 1.5 N  $HNO<sub>3</sub>$ . From a consideration of the circular morphology of etch pits, it may, however, be inferred that the reasons for the developments of these peaks are different. The modification of the morphology of  $(100)$  orientation etch pits by increasing the dilution of the acids may be the reason for the development of peaks in HCl and  $HNO<sub>3</sub>$  acids. Weakly-defined maxima in dilute  $H_2 SO_4$  may also be due to such effects. Their nature may be better understood by considering the adsorption and desorption processes.

We assume that both the acid and the reaction product adsorb on the dissolution steps. The dissolution rate for bimolecular reactions in cases when two molecules adsorb is expressed by [13]

$$
V = \frac{1}{2} S K c_{\mathbf{a}} c_{\mathbf{p}} L \tag{7}
$$

$$
V = \frac{1}{2} S K L \frac{c_a c_p}{(1 + K_{\text{eq}} c_a)^2}
$$
 (8)

and 
$$
V = \frac{1}{2} SKL \frac{c_a c_p}{(1 + K_{eq} c_p)^2}
$$
 (9)

for cases when the surface is sparsely adsorbed, the acid is more strongly adsorbed than the product, and when the product is more strongly absorbed than the acid. Here  $S$  and  $L$  have the same significance as in [13] with  $K = constant$ ,  $K_{eq} =$ equilibrium constant,  $c_a$  = acid concentration, and  $c_n$  = product concentration.

It follows from Equations 8 and 9 that the formation of a peak in every acid is, as explained above, a natural consequence of adsorption and desorption of acid and reaction product. The second peak observed in  $H_2$  SO<sub>4</sub> is associated with the concentration and viscosity effects. A relatively low value of the order of the reaction,  $n$ , may be attributed to the decreased degree of dissociation with increasing acid concentrations.

Finally some remarks should be made on the activation energy of hillock formation, dependence of the pre-exponential factor on acid concentration, and on the reported data on MgO crystals. The activation energy,  $E_h$ , of hillock formation in 27 N  $H_2SO_4$ , equal to 0.65 eV, is quite high as compared with the value 0.20 eV of the activation energy,  $E_d$ , of overall dissolution. However it is equal to the value of  $E_t$ . This means that the process of hillock formation is reaction controlled, and may be related to the reversible reaction of MgO and  $H_2SO_4$  into MgO again. At  $36 \text{ N H}_2\text{SO}_4$ , this reversible reaction does not show a systematic behaviour, as may be seen from the points given in Fig. 6.

It was remarked earlier that below 18 N  $H_2$  SO<sub>4</sub>, while the values of  $E_d$  and  $E_t$  remain constant, the values of  $A_d$  and  $A_t$  increase with increasing acid concentration, which means that  $A_d$  and  $A_t$  are functions of concentrations. The graph of  $log A_d$ and  $\log A_t$  versus  $\log c$ , illustrated in Fig. 10, shows



*Figure 10* Dependence of frequency factors  $A_d$  (curve 1) and  $A_t$  (curve 2) on H<sub>2</sub> SO<sub>4</sub> concentration c.

however that below and above  $5.5 \text{ N H}_2 \text{ SO}_4$ , they can be represented by the empirical relations,

$$
A_{\mathbf{d}} = 4.5 \times 10^{6} c^{1/5}
$$
  
\n
$$
A_{\mathbf{t}} = 5.1 \times 10^{11} c^{1/7.5}
$$
  
\nand  
\n
$$
A_{\mathbf{d}} = 2.2 \times 10^{6} c
$$
 (10)

$$
A_{\rm t} = 2.2 \times 10^{11} \; c
$$

respectively. This enables us to re-write the Arrhenius equation,

$$
K = A \exp[-E/kT] \tag{7a}
$$

into the form

$$
K = A_0 c^m \exp\left[-E/kT\right] \tag{7b}
$$

where  $A_0$  is the temperature independent part of A and the exponent,  $m$ , describing the concentration dependence has values characteristic of whether we talk of selective etching or overall dissolution, and of the concentration interval.

In order to determine dissolution rate,  $v$ , at an arbitrary point on the surface, Cabrera [19] introduced the expression

$$
v = a \gamma_{\rm s} \exp\left[-E_{\rm s}/kT\right] \tag{8}
$$

where  $\gamma_s$  is the frequency factor characterizing the frequency of nucleation,  $a$  is the height of a step  $(\sim 10^{-8}$  cm) and  $E_s$  is the activation energy of the formation of a nucleus. The frequency factor should, in principle, be a function of acid concentration and the value of  $E_s$  should depend on the nature of the acid used. In general,  $E_s$  should have different values for dissolution in  $H<sub>2</sub>SO<sub>4</sub>$ , HCl and  $HNO<sub>3</sub>$ . The values obtained of the pre-exponential factor,  $A$ , shown in Table II and Equation 6, support the concentration dependence of frequency factor, but the values of  $E_d$  and  $E_t$  (Table II) merely indicate the possibility of their dependence on the acid employed, but do not prove it unequivocally.

The values of  $E_d$  using solutions of saturated  $NH_4Cl$  and concentrated  $H_2SO_4$  in equal parts and 88%  $H_3PO_4$ , reported by Ghosh and Clarke [10], are 0.65 eV and 0.45 eV, respectively. Their value of  $E_d$  for  $H_2SO_4$  etchant is somewhat higher than that found in the present investigation but still suggests that the dissolution kinetics are reaction rate controlled in this etchant. The activation energy of dissolution  $E_d$  in the case of  $H_3$  PO<sub>4</sub> is higher than the activation energy of the viscosity decrease  $E_{\sigma}$  (Table III). This indicates that the dissolution process in  $H_3PO_4$  solution is likely to be partly diffusion controlled.

# **5. Conclusions**

(1) Spherulitic as well as dendritic patterns can be obtained by etching.

(2) The observation of peaks in etch rate versus concentration curves indicates (i) a transition from a chemically controlled mechanism to a diffusion controlled one and (ii) adsorption of the reacting and reacted species at the crystal surface. Viscosity of a solution is responsible for the diffusion limited mechanism.

(3) In  $H_2SO_4$  of concentrations less than 18 N, the dissolution process is chemically controlled with a constant value of activation energy. The dissolution rates below  $18 \text{ N H}_2\text{SO}_4$  are determined by the values of the frequency factor. At higher concentrations when the process is diffusion controlled, activation energy decides the dissolution rates. The negative and sometimes very low values of activation energy are possibly associated with the instability of reaction products.

(4) In  $H_2SO_4$  solutions with concentrations  $\leq$  18 N, the frequency factor is concentration dependent, but the dependence of the value of activation energy of dissolution on the nature of the acid, as demanded by the theory [19], has not been proved. This, however, requires more experimentation.

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